# **Electric Machinery III**

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Some slides at the end of this powerpoint were borrowed from Dr. Hani Raouf Sheybani, a lecturer at Ghochan University, and I made some changes to them. I would like to thank Dr. Raouf for his valuable contributions.

# References for Electric Machinery III

Text: A. E. Fitzgerald, Charles Kingsley, Jr And Stephen D. Umans, *Electric Machinery*. Mc Graw Hill, 7th Edition

Reference 1: P.C. Sen, *Principles of Electric Machines and Power Electronics*. Wiley, 3rd Edition

Reference 2: P.S. Bimbhra, *Electrical Machinery*. Khanna Publication

## **Electrical Machine III Syllabus**

1. Introduction

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2. Introduction to Rotating Machines

3. Generation of Sinusoidal Voltage in a Synchronous Generator

- 4. Synchronous-Machine Analyses
  - Synchronous-Machine Inductances; Equivalent Circuits
  - Steady-State Power-Angle Characteristic
  - Steady-State Operating Characteristic
  - Open- and Short-Circuit Characteristics
  - Effects of Salient Poles; Introduction to Direct and Quadrature-Axis Theory
  - Steady-State Power-Angle Characteristic of Salient-Pole Machines
  - Permanent Magnet Synchronous Machine
  - Transient Behavior of Synchronous Machine.



 $L_{ra} = P_{ra} = L_{ar} = M\cos\theta \qquad L_{rb} = L_{br} = M\cos(\theta + 120) \qquad L_{rc} = L_{cr} = M\cos(\theta - 120)$ 



Motor Configuration:

$$v_{ta} = R_a i_a + \frac{d\lambda_a}{dt}$$

Generator Configuration:

$$v_{ta} = -R_a i_a + \frac{d\lambda_a}{dt}$$

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 $E_{af}$  = Generated Voltage

 $x_{al}$  = Armature Leakage Reactance

 $x_s$  = Synchronous Reactance

 $R_a$  = Armature Resistance

 $x_{ar}$  = Armature Reaction Reactance



Motor Configuration:

 $V_a = (R_a I_a) + (j x_{al} + (j x_{ar}))I_a + (E_{af})$ 

 $V_a = R_a I_a + j x_s I_a + E_{af}$ 



With same procedure  $V_r = R_r I_r$ 

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Motor Configuration:

$$V_a = R_a I_a + (jx_{al} + jx_{ar})I_a + E_{af}$$



Generator Configuration:

$$v_t = -R_a i_a + \frac{d\lambda_a}{dt}$$

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Motor Configuration:

$$V_a = R_a I_a + (jx_{al} + jx_{ar})I_a + E_{af}$$



Generator Configuration:  $V_a = -R_a I_a - (jx_{al} + jx_{ar})I_a + E_{af}$   $E_{af} = R_a I_a + (jx_{al} + jx_{ar})I_a + V_a$ 

## **Electrical Machine III Syllabus**

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#### Steady-State Power-Angle Characteristic



$$V_a = R_a I_a + (jx_{al} + jx_{ar})I_a + E_{af}$$



Remark 1: Size of diagram? Remark 2: Comparison of  $E_r$  and  $V_a$ Remark 3: Comparison of  $E_{af}$  and  $V_a$ 

#### Steady-State Power-Angle Characteristic



**Example 1:** A 460-V, 50-kW, 60-Hz, three-phase synchronous motor has a <sup>Lecture #4-1</sup> synchronous reactance of  $x_s = 4.2 \Omega$ , stator resistance of 0.1  $\Omega$  and an armature-to-field mutual inductance, M=max(Laf( $\theta$ )) = 83 mH. Armature leakage reactance is 5% of synchronous reactance. The motor is operating at rated terminal voltage and an input power of 40 kW.

Calculate the magnitude and phase angle of the line-to- neutral generated voltage  $E_{af}$ , air gap voltage  $E_r$  and the field current  $I_f$  if the motor is operating at (a) 0.85 power factor lagging, (b) unity power factor, and (c) 0.85 power factor leading.

#### Solution (a):

$$V_{a} = \frac{460}{\sqrt{3}} < 0^{\circ}, I_{a} = \frac{40000}{\sqrt{3}460 * 0.85} < -\cos^{-1}(0.85), \quad R_{a} = 0.1\Omega, \quad x_{al} = 0.21\Omega, \quad x_{ar} = 3.99 \Omega$$

$$E_{af} = V_{a} - R_{a}I_{a} - (jx_{al} + jx_{ar})I_{a} = 265.6 < 0 - 0.1(59 < -31.8) - 4.2 < 90(59 < -31.8)$$

$$E_{r} = V_{a} - R_{a}I_{a} - jx_{al}I_{a} = 265.6 < 0 - 0.1(59 < -31.8) - 0.21 < 90(59 < -31.8)$$

$$\sum_{\text{Dr. Ali Karimpour July 2024}} \frac{15}{100}$$



Example 2: A 200-MVA , 15.75-kV, 50-Hz, three-phase synchronous Lecture #4-1

generator has a synchronous reactance of  $x_s = 2.64 \Omega$ , and stator resistance of 0.0012  $\Omega$  (r=1.1 m, g=0.1 m, l=4.62 m, N<sub>r</sub>=126(0.8 winding factor) , N<sub>a</sub>=10(0.8 winding factor) ). Armature leakage reactance is 3% of synchronous reactance. The generator is operating at rated terminal voltage and provides its rated output at 0.8 power factor lag.

a) Calculate the magnitude and phase angle of the line-to- neutral generated voltage  $E_{af}$ , air gap voltage  $E_r$  and corresponding phasor diagram.

b) Calculate the field current  $I_f$ . Solution:

$$\begin{split} &V_a = \frac{15750}{\sqrt{3}} < 0^{\circ}, I_a = \frac{200000000}{\sqrt{3}15750} < -\cos^{-1}(0.8), R_a = 0.0012\Omega, x_{al} = 0.079\Omega, x_{ar} = 2.561\Omega, \\ &E_{af} = V_a + R_a I_a + (jx_{al} + jx_{ar})I_a = 9093 < 0 + 0.0012(7331 < -37) + 2.64 < 90(7331 < -37) \\ &E_r = V_a + R_a I_a + jx_{al}I_a = 9093 < 0 + 0.0012(7331 < -37) + 0.079 < 90(7331 < -37)_{\text{Dr. Ali Karimpour July 2024}} \end{split}$$

![](_page_17_Figure_0.jpeg)

# Steady-State Power-Angle Characteristic

![](_page_18_Figure_2.jpeg)

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# Steady-State Power-Angle Characteristic

![](_page_19_Figure_2.jpeg)

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![](_page_20_Figure_2.jpeg)

# Steady-State Power-Angle Characteristic

![](_page_21_Figure_2.jpeg)

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![](_page_22_Figure_2.jpeg)

Remark: It is also valid for synchronous generator.

![](_page_23_Figure_2.jpeg)

Remark: It is also valid for synchronous generator.

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Constant active power locus in synchronous generator/motor Lecture #4-1

![](_page_24_Figure_1.jpeg)

![](_page_25_Figure_0.jpeg)

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## Steady-State Power-Angle Characteristic

Per Unit Calculation

$$S_b = ??$$
  $V_b = ??$   $Z_b = ??$ 

Ansaldo Geneartor: A 200-MVA , 15.75-kV, 50-Hz, three-phase synchronous generator has a synchronous reactance of  $x_s = 2.64 \Omega$ .

 $S_b = 200 MVA$ 

$$V_b = 15.75 \, KV$$

$$Z_b = \frac{15.75^2}{200} = 1.24 \ \Omega$$

Example 3: A 200-MVA, 15.75-kV, 50-Hz, three-phase synchronous generator-hatte

- a) Calculate the generated voltage  $E_{af}$  (Line-Line), and corresponding phasor diagram.
- b) Repeat part (a) in p.u.

Solution(a):

$$\begin{split} V_a &= \frac{15750}{\sqrt{3}} < 0^{\circ}, I_a = \frac{20000000 * 0.75}{\sqrt{3}15750} < 0 \ , R_a = 0, \ x_s = 2.64\Omega \\ E_{af} &= V_a + j x_s I_a \\ &= 9093 < 0 + (2.64 < 90)(5499 < 0) = 17130 < 58 \\ E_{af_{LL}} &= \sqrt{3}17130 = 29670 \text{ V} \end{split}$$

![](_page_27_Figure_5.jpeg)

Example 3: A 200-MVA, 15.75-kV, 50-Hz, three-phase synchronous generator-hat-1 a synchronous reactance of  $x_s = 2.64 \Omega$ , and negligible stator resistance. The generator is operating at rated terminal voltage and provides 75% of its rated output at unit power factor.

- a) Calculate the generator voltage  $E_{af}$  (Line-Line), and corresponding phasor diagram.
- b) Repeat part (a) in p.u.

Solution(b):

$$V_a = 1 < 0^{\circ}, I_a = 0.75 < 0$$
,  $x_s = \frac{2.64 \Omega}{1.24 \Omega} p.u. = 2.129 p.u.$ 

 $E_{af} = V_a + jx_s I_a$ = 1 < 0 + (2.129 < 90)(0.75 < 0)=1.884 < 58  $E_{af_{LL}} = 1.88 \ p. u. = 1.88 * 15750 = 29673 \ V$ 

![](_page_28_Figure_6.jpeg)

Different working condition for a synchronous machine

• Machine connected to an infinite bus. ( $\hat{V}_a = cte$ .)

• Machine connected to real system. ( $\hat{V}_a isn't cte$ .)

• Machine(generator) connected to a load. ( $\hat{V}_a isn't cte$ .).

![](_page_29_Figure_6.jpeg)

![](_page_29_Figure_7.jpeg)

Generator/Motor

![](_page_29_Figure_9.jpeg)

![](_page_29_Figure_10.jpeg)

Different working condition for a synchronous machine

• Machine connected to an infinite bus. ( $\hat{V}_a = cte$ .)

![](_page_30_Figure_4.jpeg)

What happens when the machine connected to infinite bus?

In this situation the terminal voltage of the machine constant.

**Example 4:** A 200-MVA , 15.75-kV, 50-Hz, three-phase synchronous generator hat a synchronous reactance of  $x_s = 2.64 \Omega$ , and negligible stator resistance. The generator is operating at rated terminal voltage(connected to infinite bus) and provides its rated output at 0.8 power factor lag.

- a) Calculate the generated voltage  $E_{af}$ , and corresponding phasor diagram.
- b) Consider that the active power is constant but rotor(field) voltage reduced by 20% draw the new phasor diagram.

 $jx_{s}I_{a}$ 

c) Consider that the active power is constant what is the minimum admissible rotor voltage.  $E_{af}$  Solution(a):

$$V_a = \frac{15750}{\sqrt{3}} < 0^{\circ}, I_a = \frac{200000000}{\sqrt{3}15750} < -\cos^{-1}(0.8), R_a = 0, x_s = 2.64\Omega$$

 $E_{af} = V_a + jx_s I_a$ = 9093 < 0 + (2.64 < 90)(7331 < -37)=25855 < 36.8

#### Solution(b): Analytical solution

 $|E_{af}| = 0.8 * 25855 = 20684$ 

$$160000000 = \frac{3 * 20684 * 9093}{2.64} \sin \delta_1 \qquad \qquad \delta_1 = 48.5^{\circ}$$

 $20684 < 48.5 = 9093 < 0 + (2.64 < 90)(I_a < \varphi_1)$ 

 $I_a < \varphi_1 = 6123 < -16.6$ 

![](_page_32_Picture_6.jpeg)

# Solution(b): Graphical solution

![](_page_33_Picture_2.jpeg)

Solution(c):

$$160000000 = \frac{3 * E_{af}^{min} * 9093}{2.64} sin90 \qquad \qquad E_{af}^{min} = 15684$$

maximum reduction of rotor voltage =1-15684/25855=0.4

![](_page_34_Figure_4.jpeg)

- Example 5: A 1.5 MW, 2300-V, unity-power-factor, three-phase, 50 Hz, 4 poles, re #4-1 Y-connected, synchronous motor has a synchronous reactance of 1.0 p.u. For this problem all losses may be neglected.
- a) Motor connected to rated voltage and working in the nominal condition. Derive phasor diagram and generated voltage in this situation.
- b) What is the breakdown torque( $T_{max}$ ) of motor?
- c) Derive torque versus power angle( $\delta$ ) characteristic and torque versus speed characteristic.
- d) Specify the power angle( $\delta$ ) for output torque of 50% of  $T_{max}$  (Note that there are two equilibrium point and just one of them is acceptable.)

Solution(a):

![](_page_36_Figure_2.jpeg)

Different working condition for a synchronous machine

• Machine connected to real system. ( $\hat{V}_a isn't cte$ .)

What happen when the machine is not connected to infinite bus?

In this situation the terminal voltage of the machine is not constant.

X<sub>EQ</sub>=0 Smaller X<sub>EQ</sub> Bigger X<sub>EQ</sub> Infinite bus A strong power network

A weak power network

![](_page_37_Figure_9.jpeg)

Generator/Motor

External system

- Example 6: A 2000-hp, 2300-V, unity-power-factor, three-phase, Y-connected;  $\mathfrak{GO}$ #4-1 pole, 60-Hz synchronous motor has a synchronous reactance of 1.95  $\Omega$ /phase. For this problem all losses may be neglected.
- a) Compute the maximum power and torque which this motor can deliver if it is supplied with power directly from a 60-Hz, 2300-V infinite bus. Assume its field excitation is maintained constant at the value which would result in unity power factor at rated load. Repeat part (a) in p.u.
- b) Instead of the infinite bus of part (a), suppose that the motor is supplied with power from a three-phase, Y-connected, 2300-V, 1500-kVA, two-pole, 3600 r/min turbine generator whose synchronous reactance is 2.65  $\Omega$ /phase. The generator is driven at rated speed, and the field excitations of generator and motor are adjusted so that the motor runs at unity power factor and rated terminal voltage at full load. Calculate the maximum power and torque which could be supplied corresponding to these values of field excitation.

Solution(a):

$$V_{a} = \frac{2300}{\sqrt{3}} < 0^{\circ} = 1328 < 0^{\circ} \qquad P = 2000 * 746 = 1492000 W$$
$$I_{a} = \frac{1492000}{\sqrt{3} \times 2300 \times 1} < \cos^{-1}(0) = 374.5 < 0^{\circ}$$
$$E_{afm} = V_{a} - jx_{sm}I_{a}$$

 $= 1328 < 0 - (1.95 < 90)(374.5 < 0) = 1517 < -29^{\circ}$ 

![](_page_39_Picture_3.jpeg)

Solving in p. u.

$$V_b = 2300 \ V \qquad S_b = 1492000 \ VA \qquad Z_b = \frac{2300^2}{1492000} = 3.5456$$
$$E_{afm} = V_a - jx_{sm}I_a = 1 < 0 - (\frac{1.95}{3.5456} < 90)(1 < 0) = 1.1413 < -29^{\circ}$$

$$|E_{afmLL}| = (1.1413)(2300) = 2625 V |E_{afm}| = \frac{2023}{\sqrt{3}} = 1517 V$$

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$$|E_{afLL}| = (1.1413)(2300) = 2625 V$$

$$P_{max} = \frac{2300 \times 2625}{1.95} \sin 90 = 3096 \text{ KW}$$

$$\omega_s = 2\pi \frac{n_s}{60} = \frac{2\pi}{60} \frac{120f_s}{p} = 8\pi$$

$$T_{max} = \frac{P_{max}}{8\pi} = 123.2 \text{ kN.M}$$

$$I_a = ??$$

$$E_{afm}$$

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Lecture HA-1

 $-jxsI_a$ 

E<sub>afm</sub>

Solution(b):

$$V_a = \frac{2300}{\sqrt{3}} < 0^\circ = 1328 < 0^\circ \quad P = 2000 * 746 = 1492000 W$$
$$I_a = \frac{1492000}{\sqrt{3} \times 2300 \times 1} < \cos^{-1}(0) = 374.5 < 0^\circ$$

 $E_{afm} = V_a - jx_{sm}I_a$ = 1328 < 0 - (1.95 < 90)(375.4 < 0)=1517 < -29°

 $E_{afg} = V_a + jx_{sg}I_a$ = 1328 < 0 + (2.65 < 90)(375.4 < 0)=1659 < 37°

$$P_{max} = \frac{3 \times 1517 \times 1659}{1.95 + 2.65} \sin 90 = 1641 \text{KW}$$

$$T_{max} = \frac{P_{max}}{8\pi} = 65.3 \text{ kN.M}$$

![](_page_41_Figure_6.jpeg)

# Exercise 1: Try to find terminal voltage and armature current in the maximum power output

![](_page_42_Figure_1.jpeg)

Load

 $X_{s}$ 

# Steady-State Power-Angle Characteristic

Different working condition for a synchronous machine

• Machine(generator) connected to a load. ( $\hat{V}_a isn't cte$ .).

![](_page_43_Figure_4.jpeg)

Assume the speed of the generator, determined by an external prime mover, is constant, but the input torque can vary.

The field winding current can be constant or adjusted by the user.

Why Might the user change the field current?

Examine the effect of load variation on terminal voltage (variation in I<sub>A</sub>).

Variation in the Magnitude of Current |I<sub>A</sub>|

Variation in the Phase of Current  $<I_A$ 

![](_page_43_Figure_11.jpeg)

![](_page_44_Figure_1.jpeg)

What is the required change in field current?

# Analytical solution?

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![](_page_45_Figure_1.jpeg)

Analytical solution?

What is the effect of increasing the load current magnitude on the phase terminal voltage of the generator for different types of loads (lagging, leading, and unity power factor) Rani Raouf Sheybani

#### Machine connected to load(Isolated generator)

![](_page_46_Figure_2.jpeg)

What is the required change in field current?

۴V

![](_page_47_Figure_1.jpeg)

Analytical solution?

What is the effect of increasing the load current phase on the phase terminal voltage of the generator for different types of loads (lagging, leading, and unity power factor)? Dr. Hani Raouf Sheybani

# Voltage regulation in synchronous Machines

$$VR = \frac{V_{\rm nl} - V_{\rm fl}}{V_{\rm fl}} \times 100\%$$

Voltage regulation in synchronous generator

A synchronous machine with a synchronous reactance of 1.28 per unit is operating as a generator at a real power loading of 0.6 per unit connected to a system with a series reactance of 0.07 per unit. An increase in its field current is observed to cause a decrease in armature current.

- a. Before the increase, was the generator supplying or absorbing reactive power from the power system?
- b. As a result of this increase in excitation, did the generator terminal voltage increase or decrease?
- c. Repeat parts (a) and (b) if the synchronous machine is operating as a motor.

#### عملا در موتورهای سنکرون در حال کار چگونه می توان توان راکتیو موتور را تنظیم کرد

| با تغییر جریان میدان 🔺 | با تغيير جريان آرميچر 🔶   |
|------------------------|---------------------------|
| هیچکدام 🔵              | با تغيير راكتانس سنكرون 📃 |

ولتار توليد شده يك زُنراتور سنكرون 2000 ولت و ولتار ترمينال أن 1800 ولت است كدام عبارت قطعا برقرار است

| ژنراتور نه توان راکتیو تولید می کند و نه مصرف   | , ژنراتور در حال مصرف توان راکتیو است |  |
|---|---------------------------------------|--|
| با داشتن زاویه بین دو ولتار امکان اظهار نظر فراهم است   | ژنراتور در حال توليد توان راکتيو است  |  |
| توان تلفاتی باد و اصطحاک یک ماشین سنکرون  |                                       |  |
| a contract to the second se |                                       |  |

| بستگی به تولید یا مصرف توان راکتیو دارد 🔺 | نمی توان اظهار نظر کرد 🔶        |
|---|---------------------------------|
| یثابت است 🔵                               | بستگی به میزان بار ماشین دارد 📃 |

ولتار توليد شده يک ژنراتور سنکرون 3600 ولت و ولتار ترمينال آن 1800 ولت است اگر زاويه بين آن دو 60 درجه باشد آنگاه

| <u>ژ</u> نراتور در حال مصرف توان راکتیو است 🔺 | با اطلاعات داده شده نمي توان اظهار نظر كرد 🔶    |
|---|---|
| <u>رُ</u> نراتور در حال توليد توان راکتيو است | ژنراتور نه توان راکتیو تولید می کند و نه مصرف 🔲 |

![](_page_51_Figure_1.jpeg)

| متناسب با جریان میدان است 🔺     | متناسب با جریان آرمیچر است 🔷                    |
|---------------------------------|---|
| با تقریب خوبی ثابت فرض می شود 🔵 | با توجه به کوچک بودن راکتانس نشتی خیلی کم است 📃 |

ژنراتور سنکرونی به ولتاژ نامی خود متصل است. تلفات اهمی سیم پیچ استاتور

| هيچكدام 🔺                       | به مجذور جریان میدان بستگی دارد 🔶 |
|---------------------------------|-----------------------------------|
| با تقريب خوبي ثابت فرض مي شود 🔵 | به جریان استاتور بستگی دارد 📃     |